# **Solution of DMS**

Set-A

# **Rajasthan Institute of Engineering & Technology, Jaipur**

Branch: - Computer Science Engineering (CSE)

# Subject: - Discrete Mathematical Structures (DMS)

**Q.1** (a) Explain the Addition Principle theorem with suitable example.

For two finite sets A and B which are disjoint, prove that

n(A U B) = n(A) + n(B)

Sol. (1) (a). Theorem – For two finite sets A and B which are disjoint, prove that

n(AUB) = n(A) + n(B)

Proof: - Let A have m1 elements than n(A)=m1 and Let B have m2 elements than n(A)=m2.

Since A and B are disjoint (having no elements in common) therefore AUB will have all the elements of A and all the elements of B.

So, numbers of elements in AUB is m1 + m2.

$$n(AUB) = m1 + m2$$
$$n(AUB) = n(A) + n(B)$$

Q.1 (b) Define the Function and Explain the Domain and Co-Domain and Range with suitable example. Sol. (1) (b)

Sol. (1) (b).

**Function** - A function is a relationship between two sets of numbers. We may think of this as a *mapping*; a function *maps* a number in one set to a number in another set. Notice that a function maps values to **one and only one** value. Two values in one set could map to one value, but one value **must never** map to two values: that would be a relation, *not* a function.

A function f is commonly declared by stating its domain X and codomain Y using the expression

 $f:X\to Y$ 

Example:

f(x) = x/2 ("f of x is x divided by 2") is a function, because each input "x" has a single output "x/2":

• f(2) = 1

• f(16) = 8

• f(-10) = -5

## **Definition of the Domain of a Function**

For a function f defined by an expression with variable x, the implied domain of f is the set of all real numbers variable x can take such that the expression defining the function is real. The domain can also be given explicitly.

## **Definition of the Range of a Function**

The range of f is the set of all values that the function takes when x takes values in the domain.

## **Definition of the Co-domain of a Function**

The Codomain and Range are both on the output side, but are subtly different.

The Codomain is the set of values that could **possibly** come out. The Codomain is actually **part of the definition** of the function.

## Example

 $\mathbf{A} = \{1, 2, 3, 4\}$ 

 $B=\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ f(x) = 2x+1

• The set "A" is the **Domain**,

• The set "B" is the Codomain,

• And the set of elements that get pointed to in B (the actual values produced by the function) are the **Range**, also called the Image.

And we have:

- Domain: {1, 2, 3, 4}
- Codomain: {1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
- Range: {3, 5, 7, 9}

## OR

**Q.1** (a) Explain the Pigeonhole Principle Theorem and also Generalized Pigeonhole Principle Theorem **Sol. (1) (a).** 

**Pigeonhole Principle -** Suppose you have k-pigeonholes and n-pigeons to be placed in them. If n > k(# pigeons># pigeonholes) then at least one pigeonhole contains at least two pigeons. In problem solving, the "pigeons" are often numbers or objects, and the "pigeonholes" are properties that the numbers/objects might possess.

**Pigeonhole Principle Theorem -** If "*n*" number of pigeons or objects are to placed in "*k*" number of pigeonholes or boxes; where k < n, then there must be at least one pigeonhole or box which has more than one object.

If k is a positive integer and k + 1 objects are placed into k boxes, then at least one of the boxes will contain two ore more objects

**Proof :** Suppose on the contrary that the proposition is false. Then, we have the case that

(i) k + 1 objects are placed into k boxes, and

(ii) no boxes contain two or more objects. From (ii), it follows that the total number of objects is at most k(since each box has 0 or 1 objects). Thus, a contradiction occurs

**Generalized Pigeonhole Principle Theorem** – If n-pigeons are sitting in k pigeonholes, where n > k, then there is at least one pigeonhole with at least n/k pigeons.

If k is a positive integer and N objects are placed into k boxes, then at least one of the boxes will contain N/k or more objects.

Here,  $\lceil x \rceil$  is called the ceiling function, which represents the round-up value of x

If N objects are placed into k boxes, then there is at least one box containing at least [N/k] objects.

Proof by contradiction: Suppose that none of the boxes contains more than [N/k] objects. Then, the total number of objects is at most [N/k]-1 objects.

$$[N/k] < (N/k)+1$$
  
  $k ([N/k]-1) < k[([N/k]+1)-1]=N$ 

This is a contradiction because there are a total of N objects.

I don't understand how that inequality shows it's a contradiction, how did they get that the inequality shows less than N objects?

Q.1 (b) Define the Constant Function and Proof the following Theorem

The logarithmic function  $f(x) = \log_{a}(x)$  is the inverse of the exponential function g(x) = axSol. (1) (b).

=> constant function :- The function f: A >B such that f(a) = C; facA and CEB is called a constant function In other words, fiA >B is a constant function if the range of contains exactly one element. then fin constant: [since sinn=0, thEA] Thearen The log anitheric function for = logue ginz = an Print - si- alogn n = n , Vn>0 and log(on) = n , Vner Now (fog) cm) = f Egens] = f Eam] = log (am) (gof) (m) = g [f (m)] = g [ (mg m] = a los co, fog(n) = n = (gof) n.This Jog and got are identity function. then fond I are the inverse of each. oduce

Q.2 (a) Define the Intersection operation of the Set and define also its properties with suitable example. Sol. (2) (a).

2> Intersection operation The intersection of two sets A and B, denoted by An defined as the set containing the elements which belong to A and defined which belong ADB = In: nEA and nEB3 And nead as "A intersection B" Verm diagram of AnB. U The intersection of a finite mins the set A, Az, An es danote à nAn = A, nA2, .... nAn : x c Ar, 1590 = 5 9 eg. if A={n:n in multiple of 33={3,6,3,12,16,34,17....? B={n:n innultiple of y 3 = {3,6,3,12,16,24,17....? AQB = [n: n is a common multiple of Band Sand 46 -> Properties of Intersection Operation 1. AAA 2.) And = 0 3.3 AnU= 4.5 And = BAA siz (AnB) nc = An(Bnc).

**Q.2** (b) What is the Set and define the Complement of a set and also define the properties with suitable example.

**Sol.** (2) (b). The present definition of a set may sound very vague. A set can be defined as a unordered collection of **entities** that are related because they obey a certain **rule**.

'Entities' may be anything, *literally*: numbers, people, shapes, cities, bits of text, ... etc

The key fact about the 'rule' they all obey is that it must be *well-defined*. In other words, it must describe *clearly* what the entities obey. If the entities we're talking about are words, for example, a well-defined rule is: X is English

The set of all elements of U (universal set) that are not elements of  $A \subseteq U$  is called the complement of A. The complement of A is

denoted by A'

 $A' = \{x : x \in U \text{ and } x \text{ not } \in A\}$ For example, Let  $U = \{a,b,c,d,e,f,g,h\}$  and  $A = \{b,d,g,h\}$ . Then  $A' = \{a,c,e,f\}$ In Venn diagram A', the complement of set A

## OR

Q.2 (a) What is Distributive Properties and explain and proof the following rules with suitable example.

 $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$ 

Sol. (2) (a).

1> Distributive property of union over interst AU(BAC) = (AUB) A(AUC). proof E(BAC) (BAC) => / MEA NEA Then and MEAUB NEA DREAWC vi (nEAUB) and ME(AUC) NEA ME (AUB) A (AUC)

**Q.2** (b) What is Set and define the Subset and its properties and Set S – T (Difference of Two Sets) with suitable example.

## Sol. (2) (b).

**Set** - A set is a collection of well-defined objects. For a collection to be a set it is necessary that it Should be well defined.

If a collection is a set then each object of this collection is said to be an element of this set. A set is usually denoted by capital letters of English alphabet and its elements are denoted by small Letters.

**For example**, A = Toy elephant, packet of sweets, magazines.

A set is represented by listing all its elements, separating these by commas and Enclosing these in curly bracket.

If V be the set of vowels of English alphabet, it can be written in Roster form as :  $V = \{a, e, i, o, u\}$ 

In this form elements of the set are not listed but these are represented by some common Property.

Let V be the set of vowels of English alphabet then V can be written in the set builder form as:  $V = \{x : x \text{ is a vowel of English alphabet}\}$ 

S-T (Difference of two sets) Set for two sets S and T, set S-T is defined as S-T = in : n as but nd TY T-S= En:not but n + 53 St S= {1,2,3, 4,5,6} and T= {5,6,7,8,9,10} then S-T= \$1,2,3,43 and T-S= {-7,8, 9,103

**Q.3** (a) Explain the Matrix Representation of graph.

Find the Adjacency Matrix of the following relation.

 $X{=}\{ \ 1 \ , \ 2 \ , \ 3 \ \} \ , \ Y{=}\{ \ 1 \ , \ 2 \ \} \ and \ R{=}\{ \ (2,1) \ , \ (3,1) \ , \ (3,2) \ \}.$ 

Sol. (3) (a).

Adjacency Matrix of a Relation :elements of sets A and B be as A = {a, a2, ... an} B= Eby, ba, --- b= 3 RIAZA then matrix of Relation es  $1, if (ai, bj) \in R$ MR = [my] man. mid = 0, id (92, 61) ER ng = matrix of Relation R or adjustens, matrix of Relation ect X = {1,2,3], Y= \$1,23 and R = \$62,10, (3,10) (3,2) J then mp on a 3×2 matrix, comos anto d. other elements are all ze unity and other all you me = Find the relation R; when Cr. 0 0 mp -0.0 0 Rix-34 relation inother -160 Z con, y=>, con, y=>, con, y=>, con, i, ), (n=, i), (n=, i))

Q.3 (b) Define the Join and Meet of Boolean Matrices. Also Perform the Join and Meet operation of following Two Boolean Matrices. Sol. (3) (b).

\* Jain and Meet of Bralean Materices -Let A - Eag I wan and B = [big ] wan be time Bookens The join of A and B, denoted by AVB E, a making id a is = 1 or bit = 1 Cii = if aij = 0 = bij IAVB =C The meet of A and B, denoted By AAB, is a matrix D = [ dij ] myn wh it ag = 1 = 6:5 I ary = 0 or hig = 0 I ANB = DI -----\* The join and meet of two Burlean matrix are also Baolean mabices eg. computer the join and whet a) the methices 0 0 1 A B-0 ï O T 1 100 03 0 co. 0 63 1 0 C= AVB-. 0 O D= AAB -. 1 . 0 1 0 0 ٠ 0 Ó D. 0 1 . . 0 0 1

**Q.3** Explain the Recursive definition of a Set with suitable example. Also define Power Set with suitable example.

Sol. (3)

-> Recursive Definition of A set :-An objects can be defined in terms of itself. This process on called Recursive. A necursive definition of a set 5 consists of Hare clauses: 1.2 Basis clause - explicitly lists atleast one dent en S. 2) Recursive clause - provides suches used to generate new elements of the set & from the known elements. 3) Terminal clause - ensures that the first two clause are the only means to determine the cloments of S.

-> Power Set: - The set of all subsets of a give set s in called the power set of s and demoted by P(S). i.e. R(S) = ST: TSSY bothe member of P(S). d and 5 ame Let 5 = 20,53 then P(S) = { 203, 253; 2053, 4

Q.4 Define the following functions with examples:Q.4 (i) Floor and Ceiling functionsSol. (4) (i).

-> 5. Floor function or Connectest Integer function set of real number -then the he the -the floor function I: R calle cf&f(n) Fh x by en flight tha \* interer. longest equal to X 51=5. 1-9.2 -10 7 . 1 2 R.91 · Function: 26.7 function A said to be the ceiling dar fern ctio g (n) the X it integer that & greater term correct to 51-1000 : FITI=17en 18.57 = 3 F-5.3] = - 5 it be any real meister and a Let 1828 12716 ---any indege There (n#=) - if it is add vy 2 mal vis [m/2] = more , if n is add

Q.4 (ii) Div and Mod functions. Sol. (4) (ii).

-> 8 > Div Function :-The div function on divy. denoted by div (n, 1), is the quotient when n is divided the remainder should be non-negative. div(22,5)= 22 div5=4 div (5,6) = 0. we can define the other operators in terms of the div operator as follows a1 = div (9,6). is Floor function eg. div(23,5) = 4 and 122 = - div (-a, 5) is cailing function [9] 29. [23] -5 Stone - div (-23, 5) = - [quotient when (-25+2). divided by 56 to make mensioned - - (-s) = s. 372 mod Function The mud function n mod y demotes the grander an integer divided by a positiv n co integer y. CH 1211 mod 5 = 41 eg. mud (15,3) = 15 mod 3 = 0 the mad function can be used in days for a given particular days to Today as Tuesday, what day of the u sult - interna, su St = 1 too man and 7 - - 2 2nd day from duday (is Thereday) in Thursday Three it tros dery

**Q.4** Define the following terms with examples: (i) Equal set and Universal set.

**Sol.** (4)(i)

Equal sets: - when two sets S and T and consists of the same clement, they called equal and we shall write ave DATE .... if s and T are not equal, we shall g = T-STT. awrites so when S= [Ram, Shyan, Mohany T = [ Mahan, shyam, Ram] then S=T. concertant = 21, 2, 33 and T= 22, 1, 1, 2, 2, 3, 1, 3 3 the ST. when S = 21, 2, 35, and T= 20, 1, 2, 33 S = T. since O is an element of T but not of s.

> Universal Set : - If all the sets under consideration are subsets of a fixed set, then this fixed set is called universal set and denoted by U. then U is the Universal set for Band T.

Q.4 (ii) Finite set and Infinite set. Sol. (4)(ii)

> Finite set :- A set is said to be a finite set if the rember of its distinct = set s= [n: new and new y is a finites -> Infinite Set :- A set having infinite number of distinct elements is called the infinite set. Set S= EnINEN and N>103 is an infinitesol.

# **Solution of DMS**

# **Rajasthan Institute of Engineering & Technology, Jaipur**

Branch: - Computer Science Engineering (CSE)

### Subject: - Discrete Mathematical Structures (DMS)

**Q.1** (a) Explain the Addition Principle theorem with suitable example.

For two finite sets A and B, prove that

 $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ 

### Sol. (1)(a)

=> Addition Principle :-Theorem - for two finite sets A and B ashick are disjoint, prove that m(AUB) = m(A) + m(B).Proot : A have my elements they m(A) = my Let and B have my claments than m(B)=mg since. A and B are disjoint (having edements in common) the for will have all the elementer A as all the cloments of B. So wimber dements in AUB is my ung  $m(AUB) = m_1 + m_2$ n(AUB) = n(A) + n(B). Groved. Prove Jer dinite sets A and B Theorem  $m(A \cup B) = m(A) + m(B) - m(A \cap B).$ we know that Price ---(A-B) U(AAB) U(B-A) = AUB A-B, AAB and B-A are pair wis disjoint, then done.  $n(A \cup B) = n(A - B) + n(A \cap B) + n(B - A) - (B)$ A= (A-B) V(AAB). Juthor CA-B) A (AAB) = Ø = n(A) = n(A-B) + n (A nB) --- 3 n(a) = n(AAB) + n(B-A)OD

adding eg - (D) and CD. n(A) + n(B) = {n(A-B) + n(AAB) + n(B-A)}+ En(ANB)-> m(AUB) + m(ANB) [win man) + man) - mana) IDOB AVB IP) m that is the condinality of AUB derived by including tothe. and exclud condinality of AnB. principle the addition · es Principle of lead Inclusion Icania m

 $\mathbf{Q.1}$  (b) Explain the Generalized Pigeonhole Principle Theorem With suitable example.

# Sol. (1)(b)

**Generalized Pigeonhole Principle Theorem** – If n-pigeons are sitting in k pigeonholes, where n > k, then there is at least one pigeonhole with at least n/k pigeons. If k is a positive integer and N objects are placed into k boxes, then at least one of the boxes will contain N/k or more objects. Here,  $\lceil x \rceil$  is called the ceiling function, which represents the round-up value of x. If N objects are placed into k boxes, then there is at least one box containing at least  $\lceil N/k \rceil$  objects.

**Proof by contradiction:** Suppose that none of the boxes contains more than [N/k] objects. Then, the total number of objects is at most [N/k]-1 objects.

$$[N/k] < (N/k)+1$$
  
  $k([N/k]-1) < k[([N/k]+1)-1]=N$ 

This is a contradiction because there are a total of N objects.

I don't understand how that inequality shows it's a contradiction, how did they get that the inequality shows less than N objects?

5 separate departments in a department 29) and dotal no of employee are 15 that one of the departments must least 3 employee. 36 employee are pigeon and supported compluy ees da-+1 = 7+1=B.

# **Q.1** (a) Define Constant Function, Equal Function and Identity Function with suitable example. **Sol. (1)(a)**

**Constant Function -**

=> constant function :- The function f: A->B such that flat = C; fach and CEB is called a constant function To other words, fiA >B is a constant function if the range of f contains exactly one element. eg: if A = { TI, 2T, 3TI and f(x) = Sinn, nEA then fier constant. Crince sinn=0. UNEA].

**Equal Function** –

=> Equal Function : -Two functions of and gave said to be equal iff -1) the domain of f = the domain of g. 2) the co-domain of f = the co-domain of g 3) f(n) = g(n) for every n belonging to their common domain Ict A = £1,23, B= £3,63
J: A→B ; J(n) = x<sup>2</sup>+2 9. A-0B; 9000 = 3h  $f(1) = 3 = g(1) \frac{2}{3}$  $f(2) = 6 = g(2) \frac{2}{3}$ 

### OR

**Identity Function -**

> Identity Function :-A function of : A > A in said to be an identity function of A if f associates every dement of A to the element itself. f: A > A is an identity iff f(n) = n, thEA

**Q.1** (b) Define the following function with suitable example.

(i) Polynomial Function

### Sol. (1)(b)(i)

**Polynomial Function-**

A function of: R > R at the form  $f(n) = a_n x^n + a_n x^{n-1} + \dots + a_n x + a_n$ where at GR, i=1 ton and an = 0 in called a polynomial function of degree is for n=1,  $f(n) = a, n + a_0$  (linear function) for n=2,  $f(n) = a_2n^2 + a_1n + a_0$  (quadratic function).

Q.1 (b) (ii) Exponential Function Sol. (1)(b)(ii) Exponential Function –

=> Equal Function : -Two functions of and gave said to be equal iff -1.) the domain of f = the domain of g. 2.) the co-domain of f = the co-domain of g. 3.) f(m) = g(m) for every n belonging to their domain . common Sop let A = {1,23, B= } 3,63  $\frac{1}{9} : A \rightarrow B ; \frac{1}{9} : \frac{1}{9$ f(1) = 3 = g(1) ? f(2) = 6 = g(2) ?

> Proporties of Exponential function The exponential function f(n) = an 1) down (f) = (-0, 00); Hauge (f) = (0,00) y-intercept of the spops is then n, > n2 => f (n, )>f (na) 22>1 franction o f és an increasing - ocaci, then n, then > for, ) of out is a decreasing havizonta asymptote 100 the graph methods af each other y-anis an ar and (an) - and an+3

**Q.2** Explain the following term with suitable example.

(i) Singleton Set

- (ii) Disjoint Set
- (iii) Partition of the set.(iv) Cardinality of A Finite set.(v) Set of Sets.
- Sol. (2)(i) Singleton Set -

-> Singleton Set or Singleti- A only are clement is known as singleton set or simply singlet. 5:= 263.

Sol. (2) (ii) Disjoint Set –

Disjoint Set :- Two set S and T are said be disjoint when they have no element common, i.e. when no element of S is and no element of Terins. 14 and the the second ey. Let S be the set Eq. S, cy and T be the set Le, f, gj. Then S and T are disjoint.

Sol. (2) (iii) Partition of the set -

=> Partitions of set :- A Set 1 A set EA, B. C.-7 of non-empty enderts of a set s it in AUBUCU is-the AnBACA. - - - - - - - - - - - + the intersection of every peir of Alstinet subsets is the emptyd where the subset D, B.C ... are called its member (element) or blocks. sert 3,6.3,12, B= \$ 1, 4, 7, 10, - --a= 5 2, 5, 8, 11 233 5=51,2,3, the AUBUC = S. and AAB = AAC = BAC = Ø - EARB, C.J. in a partition of Set SA

**Sol.** (2) (v) Set of Sets.-

A set itself many may some. times be an element of another set. Then the latter set is called the set of set.

Q.3 (a) Define the Comparable and Non-Comparable set with suitable example. Sol. (3)(a)

> Comparable Sets: - Two sets Sand Tare Seun to be comparable if set or Tes. i.e. One the sets is a subset of the other. eq. S= {1,2,34 and T= {1,2,3,44. Then S is comparable to To became Se -> Non-Comparable set :-Two set Sand hour comparable if SOT said to i.e. none of the set is subset 04 other. s={0,by, T={b, d, e}. \$T and T\$S. the S and T ave not comparable.

Q.3 (b) What is the Function? Define the f-image, f-set and Representation of function by a diagram.Sol. (3)(b)

Function –

-> Functions (or mapping sets. Let there two given Let A and & are a rule denoted by f, which associate element of A, a unique. element of B. called a function or mapping from It is denoted by neads of is a function from A to A to B.

# f-image -

> f-image :-Element b (EB) corresponding to element a CEA) will be denoted ! symbol f(a) and in called fining the of a.

f-set -

The set formed by all the >-f-set :e of the elements of A coulded -) he image - set and as denoted fCAD.

Representation of function by a diagram-

-> Representation by a diagram :-The mapping or Junction J: A->B is said to has an image for an B every element a CA A EA has andy one image Jeas 2) an element en B. But, it is possible that two or more elemants a EA ( Say a, a, a, ... ) may have the same image on B. i.e. f (91) = f(92) = f (92). The mapping or function fin the may be represented by a diagram. · 60 A= [3,4,5], B= [7,8,9], f(3) = 8, fa)3 TI f(s)=7, f(s)=8, find out whether a mapping. go does not define a mapping asthe 7.8 of B are the imaget 9/42 element same clement sof A.

 $\mathbf{Q.3}$  (a) Explain the Matrix Representation of graph.

Find the Adjacency Matrix of the following relation.

 $X{=}\{ \ 1 \ , \ 2 \ , \ 3 \ \} \ , \ Y{=}\{ \ 1 \ , \ 2, \ 3 \ \} \ \text{and} \ R{=}\{ \ (1,3) \ , \ (1,2) \ , \ (2,1) \ , \ (3,1) \ , \ (3,2) \ , \ (3,3) \ \}.$ 

# **Sol.** (3)(a)

 $\mathbf{Q.3}$  (b) Define the Join and Meet of Boolean Matrices. Also Perform the Join and Meet operation of following Two Boolean Matrices.

**Sol. (3)(b)** 

t The join and meet of two Boolean matrix and als o Baolean mabices computer C.C.)the join and weet of the methices 0 0 A R-0 0 C3 ð 0 63 1 C= AVB= . 0 O D= ANB . . . 0 1 0 0 . 0 Ó 0 D 1 . . 0 0 1

**Q.4** (a) What is the function? Explain the Equal Function and Sum and Product of Function with suitable example.

# Sol. (4)(a)

# **Function** -

-> Functions (or mapping) :two given sets. Let there enis Let A and Q are a rule denoted by f, which associate to each element of A, a unique element of B. Then f mapping from A to called a function or It is denoted by 132 152 3 A->B reads of is a function from A to B A to B. aps

# **Equal Function** –

Equal Function : Two functions of and gave said eto equal iffthe der of 1 = domain of 1-2 the - domain of 27 -74 60 Co-domas f = thegen for every n. belonging 3.) domain nmon A= 21,23 , B= 3.63 Let Sop A-B  $1 - (n) = n^2 + 2$ 8000 A-PB = 34 f(1) = 3 = g(1)1(2)=6=9(2

Sum and Product of Function –

> Sum and Product of Function Let f: A -> R and g: B -> R be two function. Then their sum f +9 and product fg can be defined on below (f+g) (n) = f(n) + g(n). (fg) (n) = f(n). g(n). dom(f+g) = dom(fg) = dom(f) n dem(g) are down (f) = (-co, co) and down (g)=[1, co The abtain the sum and product of fair (f+g)(n) = f(n) + g(n)=  $n^2 + \sqrt{n-1}$ (fg) (n) = for, g(n). = nº. Jn-1 1 dom (g) = [1, 00] dom find and good are defined only dom (f+9) = dom (f9) =

**Q.4** (b) Explain the Logarithmic function and also define the Properties of Logarithmic function. **Sol. (4)(b)** 

-> 3> Logarithmic Functions:-Let a ( = 1) E Rt and N, y E R such that y= an Then me called begarithen of J. n = log y (> y = an These states function of : RT -> R defined by for = log n as the logarithmic function with base a. since and so y = and is always positive for every nER since can say that n= log y is defined any the domain of legarithmic function is (0, a) and its stange is (- on, as). Three bases of legrithms, namely e, 2 and 10. are often used. log n = On n Enatural logeritting] log n = egn Lcommonly used in computer log n = log n [bare 10 is usually amitted 010 -> Properties of Logarithmic Functions Logorithmic function for = log n. 1> dom(f) = (0,00) grange (f) = (-a,00). 2> The n-intercept of the legarithmic graph 1 3> for a>1, of increasing. adadi, of in decreasing Aur 43 Y-anis & a vertical asymptote of the graph. sig fins = log n and gens = an are invarce of cach atter and their graphs are minter I mane of each other about the line J=r. as the graphic of y = log n and y = log n are reflection of each other about the X-anis thearent let a( =1), b(=1), n and y are any positive weal number and maner then.

**Q.4** (a) Explain the Absolute Value Function and Characteristic function with suitable example.

### Sol. (4)(a)

## **Absolute Value Function -**

-> 40 Absolute Value Function :-The function of : R > R defined by - fens = 1n1 = { - x, x <0 is called absolute value function. The graph of the function y= MI or as show. dist 1/10 - 2:60-4 7=11 is 1-2-6-407 = 1-2+41=2 1>1-2-51 = 1-71=7. 5450 450 |-2| = -(-2) = 213 = 3 ; 1-81 = 8; the absolute value fi is used to measure

### **Characteristic function -**

->>> characteristic function :-Let Acbe a subset of the Universale set U = { u, u, u, u, u, uny The characteristic function of A in defined as a jusction from U to 20,13. i.e.  $U \rightarrow \{0,1\}$ .  $f(u_i) = \int 1, if u_i \in A$ U→ 20,13. by the This prettion is used in supresenting sets in computor. Sequence af o's and I's of sent the equal to the cardinality of U because OFA and IEA. = IJ U= E1,2,3,4,5,6,7, 8, 3, 103 A= E3,43, B= 29, 687, C= E6,8, 109 then f (m) = { 1, when n = 3, or y de corresponds to sequence = 0,0,0,1,0,1,0,1,0,0. de corresponds to requence = 0,0,0,0,0,0,0,0,0,1,0,1.

**Q.4** (b) Define the following term with suitable example.

# Sol. (4)(b) (i) Bijection Mapping

A-) 1 ng Mapping. -> S.> Bijection ON Sizection c. 20 to 60 Saud in well as onto wapping (B) -(9)= Bijection & (A) N+1 : Z > Z (n) manny eq. use for any bujec 2CCar +10= No Cr - one en ane an 10

Sol. (4)(b) (ii) One-One Mapping.

One - One map 17 aneer said Amappin event element of hand dic mage en B. This. ever (a) = f(b)acb, -one 9.5 RA Fb =)+( -(5) a set of integers I de the 201. all even integer 0 e sel al , dephes mapping 60 athic one - and n injection finz=-n. Then Eg. 976= ez fer any 9,0 peconne 1(9) + + (6),

Sol. (4)(b) (iii) Onto Mapping.

->2> Onto Mapping (or Surjective Ma Ead A-B es such ping or Image. 2 or A, t e ment 01 mapping Con 0 (A) =44 and BE 20 dhen. NEA ele a 10 is 0 0